

SOLUTIONS

SAMPLE QUESTION PAPER - 1

Solved _____

Time : 3 Hours

Maximum Marks : 90

SECTION 'A'

1. (C) $\frac{\sqrt{98}}{\sqrt{2}} = \sqrt{\frac{98}{2}} = \sqrt{49} = 7$ 1
2. (B) $x + 4$ is a factor of $x^2 + 3x + m$
 $\Rightarrow p(-4) = 0$
 $\Rightarrow (-4)^2 + 3(-4) + m = 0$
 $\Rightarrow 16 - 12 + m = 0$
 $\Rightarrow m = -4$ 1
3. (C) If, $x + y + z = 0$
 then, $x^3 + y^3 + z^3 = 3xyz$
 Hence, $x^3 + y^3 + 8 = 3(x)(y)(2)$
 $= 6xy$ 1
4. (B) Degree of polynomial $\sqrt{3}$ is zero. 1

SECTION 'B'

5. $x = 3 - 2\sqrt{2} \Rightarrow \frac{1}{x} = 3 + 2\sqrt{2}$ $\frac{1}{2}$
- $\left(\sqrt{x} + \frac{1}{\sqrt{x}}\right)^2 = 8$ 1
- $\sqrt{x} + \frac{1}{\sqrt{x}} = \pm 2\sqrt{2}$ $\frac{1}{2}$

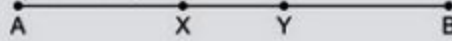
[CBSE Marking Scheme, 2012]

6. $x^4 - y^4 = (x^2)^2 - (y^2)^2$ $\frac{1}{2}$
 $= (x^2 - y^2)(x^2 + y^2)$ $\frac{1}{2}$
 $= (x - y)(x + y)(x^2 + y^2)$ 1

[CBSE Marking Scheme, 2012]

7. $(x + 2)$ is a factor of $p(x) = 2x^3 - kx^2 + 3x + 10$ ½
 $\Rightarrow p(-2) = 0$
 $\Rightarrow 2(-2)^3 - k(-2)^2 + 3(-2) + 10 = 0$ 1
 $\Rightarrow -16 - 4k - 6 + 10 = 0$
 $k = -3$ [CBSE Marking Scheme, 2014] ½

8. Let AB has 2 mid points, say X and Y , then

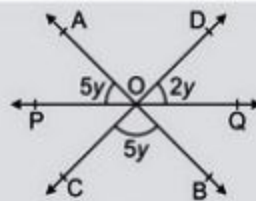


Then $\frac{AB}{2} = AX$ and $\frac{AB}{2} = AY$ ½
 $\therefore AX = AY$ (Things which are equal to the same things are equal to one another) ½
Hence, X and Y coincide. Thus, every line segment has one and only one mid point ½
[CBSE Marking Scheme, 2013, 12, 11]

9. Let the two supplementary angles are $2x$ and $3x$, then

$2x + 3x = 180^\circ$
 $\Rightarrow x = \frac{180^\circ}{5} = 36^\circ$ 1
Hence, the angles are $2x$ and $3x$ or 72° and 108° . [CBSE Marking Scheme, 2012] 1

OR



$\therefore \angle POC = 2y$, (Vertically opp. angles) ½
 $5y + 2y + 5y = 180^\circ$ (AOB is a st line) ½
 $12y = 180^\circ$ ½
 $y = 15^\circ$. [CBSE Marking Scheme, 2012] ½

10. $s = \frac{120}{2} = 60$ ½

Sides = $5x + 12x + 13x = 120$

$30x = 120$ ½

$x = 4$ cm

$5x = 20$ cm, $12x = 48$ cm, $13x = 52$ cm.

Area of $\Delta = \sqrt{s(s-a)(s-b)(s-c)}$ sq. cm ½
 $= \sqrt{60 \times 40 \times 12 \times 8} = \sqrt{230400}$
 $= 480$ cm² [CBSE Marking Scheme, 2012] ½

SECTION 'C'

11. $\frac{4}{3\sqrt{3}-2\sqrt{2}} + \frac{3}{3\sqrt{3}+2\sqrt{2}} = \frac{4(3\sqrt{3}+2\sqrt{2})+3(3\sqrt{3}-2\sqrt{2})}{(3\sqrt{3}-2\sqrt{2})(3\sqrt{3}+2\sqrt{2})}$ ½
 $= \frac{12\sqrt{3}+8\sqrt{2}+9\sqrt{3}-6\sqrt{2}}{27-8}$ ½

$$\begin{aligned}
 &= \frac{21\sqrt{3} + 2\sqrt{2}}{19} && \frac{1}{2} \\
 &= \frac{21 \times 1.732 + 2 \times 1.414}{19} && \frac{1}{2} \\
 &= \frac{36.372 + 2.828}{19} && \frac{1}{2} \\
 &= \frac{39.2}{19} = 2.063. && \frac{1}{2}
 \end{aligned}$$

[CBSE Marking Scheme, 2012]

OR

$$\begin{aligned}
 x &= \frac{1}{p} = \frac{1}{5+2\sqrt{6}} = \frac{1}{5+2\sqrt{6}} \times \frac{(5-2\sqrt{6})}{(5-2\sqrt{6})} && \frac{1}{2} \\
 &= \frac{5-2\sqrt{6}}{25-24} = 5-2\sqrt{6} && \frac{1}{2} \\
 p^2 + x^2 &= (5+2\sqrt{6})^2 + (5-2\sqrt{6})^2 && \frac{1}{2} \\
 &= (5)^2 + (2\sqrt{6})^2 + 2 \times 5 \times 2\sqrt{6} + (5)^2 + (2\sqrt{6})^2 - 2 \times 5 \times 2\sqrt{6} && \frac{1}{2} \\
 &= 25 + 24 + 20\sqrt{6} + 25 + 24 - 20\sqrt{6} && \frac{1}{2} \\
 &= 98. && \frac{1}{2}
 \end{aligned}$$

[CBSE Marking Scheme, 2012]

12.

$$\begin{aligned}
 \frac{5+\sqrt{3}}{7-4\sqrt{3}} &= \frac{5+\sqrt{3}}{7-4\sqrt{3}} \times \frac{7+4\sqrt{3}}{7+4\sqrt{3}} = \frac{35+20\sqrt{3}+7\sqrt{3}+12}{49-48} \\
 &= \frac{47+27\sqrt{3}}{1} && 1 \\
 \frac{5+\sqrt{3}}{7+4\sqrt{3}} &= \frac{(5+\sqrt{3})(7-4\sqrt{3})}{(7+4\sqrt{3})(7-4\sqrt{3})} = \frac{23-13\sqrt{3}}{1} && 1 \\
 \therefore \frac{5+\sqrt{3}}{7-4\sqrt{3}} - \frac{5+\sqrt{3}}{7+4\sqrt{3}} &= (47+27\sqrt{3}) - (23-13\sqrt{3}) \\
 &= 24+40\sqrt{3} && 1
 \end{aligned}$$

[CBSE Marking Scheme, 2012]

13. $27p^3 - \frac{1}{216} - \frac{9}{2}p^2 + \frac{1}{4}p$

$$\begin{aligned}
 &= (3p)^3 - \left(\frac{1}{6}\right)^3 - 3(3p)^2 \left(\frac{1}{6}\right) + 3(3p) \left(\frac{1}{6}\right)^2 && 2 \\
 &= \left(3p - \frac{1}{6}\right)^3 && \frac{1}{2} \\
 &= \left(3p - \frac{1}{6}\right) \left(3p - \frac{1}{6}\right) \left(3p - \frac{1}{6}\right) && \frac{1}{2}
 \end{aligned}$$

[CBSE Marking Scheme, 2010, 2011, 2012]

OR

$$\begin{aligned} \left(\frac{x}{3} + \frac{y}{5}\right)^3 - \left(\frac{x}{3} - \frac{y}{5}\right)^3 &= \left[\frac{x}{3} + \frac{y}{5} - \frac{x}{3} + \frac{y}{5}\right] \\ &\quad \left[\left(\frac{x}{3} + \frac{y}{5}\right)^2 + \left(\frac{x}{3} - \frac{y}{5}\right)^2 + \left(\frac{x}{3} + \frac{y}{5}\right)\left(\frac{x}{3} - \frac{y}{5}\right)\right] \quad 1 \\ &= \left(\frac{2y}{5}\right) \left[\frac{x^2}{9} + \frac{y^2}{25} + 2 \times \frac{x}{3} \times \frac{y}{5} + \frac{x^2}{9} + \frac{y^2}{25} - 2 \times \frac{x}{3} \times \frac{y}{5} + \frac{x^2}{9} - \frac{y^2}{25}\right] \quad 1 \\ &= \frac{2y}{5} \left[3 \times \frac{x^2}{9} + \frac{y^2}{25}\right] \quad \frac{1}{2} \\ &= \frac{2y}{5} \left(\frac{x^2}{3} + \frac{y^2}{25}\right) \quad \text{[CBSE Marking Scheme, 2011]} \quad \frac{1}{2} \end{aligned}$$

14.

Factors of -6 are $\pm 1, \pm 2, \pm 3, \pm 6$

Now,

$$f(x) = x^3 - 6x^2 + 11x - 6$$

$$\begin{aligned} f(1) &= (1)^3 - 6(1)^2 + 11(1) - 6 \\ &= 1 - 6 + 11 - 6 = 0 \quad 1 \end{aligned}$$

$$\begin{aligned} f(-1) &= (-1)^3 - 6(-1)^2 + 11(-1) - 6 \\ &= -1 - 6 - 11 - 6 \neq 0 \end{aligned}$$

$$\begin{aligned} f(2) &= (2)^3 - 6(2)^2 + 11(2) - 6 \\ &= 8 - 24 + 22 - 6 = 0 \quad 1 \end{aligned}$$

Similarly,

$$\begin{aligned} f(-2) &\neq 0 \\ f(3) &= (3)^3 - 6(3)^2 + 11(3) - 6 \\ &= 27 - 54 + 33 - 6 = 0 \quad 1 \end{aligned}$$

and

$$f(-3) \neq 0$$

Hence, $(x-1)(x-2)(x-3)$ are the factors.

15. Join AC



$$\text{Ext. } \angle 4 = \angle ACB + \angle CAB \quad \dots(i) \quad \frac{1}{2}$$

$$\text{Ext. } \angle 3 = \angle DAC + \angle DCA \quad \dots(ii) \quad \frac{1}{2}$$

Again,

Adding (i) and (ii), we get

$$\begin{aligned} \angle 3 + \angle 4 &= (\angle ACB + \angle DCA) + (\angle CAB + \angle DAC) \quad \frac{1}{2} \\ &= \angle 1 + \angle 2 \end{aligned}$$

$$\therefore \angle 3 + \angle 4 = \angle 1 + \angle 2. \quad \frac{1}{2}$$

[CBSE Marking Scheme, 2012]

OR

In $\triangle ABC$, $\angle A + \angle B + \angle C = 180^\circ$ (Angle sum property)

$$90^\circ + \angle B + \angle C = 180^\circ \quad (\angle A = 90^\circ)$$

$$\therefore \angle B + \angle C = 90^\circ$$

$$\therefore \angle C = \angle ACB = 90^\circ - \angle B \quad \dots(i) \quad 1$$

Also, in $\triangle ALB$,

$$\angle ALB + \angle BAL + \angle B = 180^\circ$$

(Angle sum property)

$$90^\circ + \angle BAL + \angle B = 180^\circ$$

1

$$\angle BAL = 90^\circ - \angle B$$

...(ii) $\frac{1}{2}$

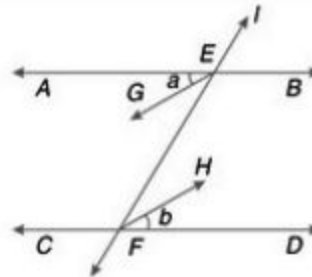
Hence, from (i) and (ii), we get

$$\angle BAL = \angle ACB$$

$\frac{1}{2}$

[CBSE Marking Scheme, 2012]

16.



EG is the bisector of $\angle AEF$

\therefore

$$\angle AEG = \angle GEF = a$$

Similarly,

$$\angle EFH = \angle HFD = b$$

$\frac{1}{2}$

\therefore

$$\angle GEF = \angle EFH$$

($\because a = b$) $\frac{1}{2}$

But these are alternate interior angles

\therefore

$$EG \parallel FH$$

$\frac{1}{2}$

Again,

$$\angle AEF = 2a$$

$\frac{1}{2}$

and

$$\angle EFD = 2b$$

$\frac{1}{2}$

\therefore

$$\angle AEF = \angle EFD = 2a \text{ or } 2b$$

$\frac{1}{2}$

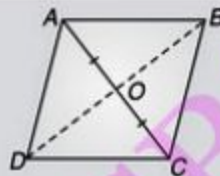
But these are alternate angles.

\therefore

$$AB \parallel CD.$$

$\frac{1}{2}$

17.



Join OD and OB.

In $\triangle AOB$ and $\triangle COB$,

$$AO = CO$$

(Given) $\frac{1}{2}$

$$OB = OB$$

(Common)

$$AB = BC$$

($\because ABCD$ is a rhombus)

$$\triangle AOB \cong \triangle COB$$

(SSS Congruence.)

$$\angle AOB = \angle COB$$

(By c.p.c.t.) ... (1) $\frac{1}{2}$

Similarly,

$$\triangle AOD \cong \triangle COD$$

$\frac{1}{2}$

$$\angle AOD = \angle COD$$

(By c.p.c.t.) ... (2) $\frac{1}{2}$

$$\text{But, } \angle AOD + \angle COD + \angle COB + \angle AOB = 360^\circ$$

$\frac{1}{2}$

$$2(\angle AOD + \angle AOB) = 360^\circ$$

$\frac{1}{2}$

$$\angle AOD + \angle AOB = 180^\circ$$

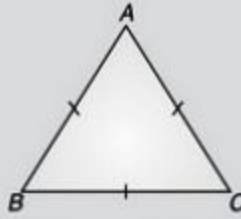
$\frac{1}{2}$

$\Rightarrow D, O, B$ are collinear.

$\frac{1}{2}$

[CBSE Marking Scheme, 2012]

18.

 \therefore

$$AB = AC \quad [\text{sides opposite of equal angles are equal}] \quad \frac{1}{2}$$

$$\angle B = \angle C = x$$

$$BA = BC$$

[....do.....]

 \therefore

$$\angle A = \angle C = x$$

Also,

$$AC = BC$$

 $\frac{1}{2}$

$$\angle A = \angle B = x$$

[....do.....]

But,

$$\angle A + \angle B + \angle C = 180^\circ$$

[Angle sum property] $\frac{1}{2}$

$$3x = 180^\circ$$

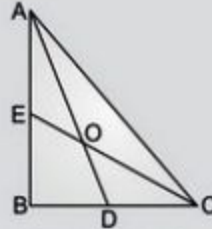
$$x = 60^\circ$$

 $\frac{1}{2}$ \therefore

$$\angle A = \angle B = \angle C = 60^\circ.$$

 $\frac{1}{2}$

[CBSE Marking Scheme, 2012]

19. In $\triangle ABC$,

$$\angle A + \angle B + \angle C = 180^\circ$$

[Angle sum property] $\frac{1}{2}$

$$\angle A + \angle C = 180^\circ - \angle B = 180^\circ - 90^\circ = 90^\circ$$

 $\frac{1}{2}$

$$\frac{1}{2}(\angle A + \angle C) = 45^\circ$$

 $\frac{1}{2}$ In $\triangle AOC$,

$$\frac{1}{2} \angle A + \frac{1}{2} \angle C + \angle AOC = 180^\circ$$

 $\frac{1}{2}$

$$45^\circ + \angle AOC = 180^\circ$$

 $\frac{1}{2}$

$$\angle AOC = 180^\circ - 45^\circ = 135^\circ.$$

[CBSE Marking Scheme, 2012] $\frac{1}{2}$

20. For triangle,

$$s = \frac{a+b+c}{2} = \frac{26+28+30}{2} = \frac{84}{2} = 42$$

 $\frac{1}{2}$

$$\text{Area of } \Delta = \sqrt{s(s-a)(s-b)(s-c)}$$

 $\frac{1}{2}$

$$= \sqrt{42(42-26)(42-28)(42-30)}$$

$$= \sqrt{42(16)(14)(12)}$$

$$= \sqrt{2 \times 3 \times 7 \times 4 \times 4 \times 7 \times 2 \times 2 \times 2 \times 3}$$

 $\frac{1}{2}$

$$= 2 \times 2 \times 3 \times 4 \times 7$$

$$= 336 \text{ cm}^2$$

 $\frac{1}{2}$

$$\text{Area of parallelogram} = \text{Area of triangle}$$

(Given)

$$b \times h = 336$$

 $\frac{1}{2}$

$$28 \times h = 336$$

$$h = 12 \text{ cm.}$$

[CBSE Marking Scheme, 2012] $\frac{1}{2}$

SECTION 'D'

21.
$$\frac{1}{1+x^{a-b}} + \frac{1}{1+x^{b-a}} = \frac{1}{1+\frac{x^a}{x^b}} + \frac{1}{1+\frac{x^b}{x^a}} \quad 1$$

$$= \frac{1}{\frac{x^b+x^a}{x^b}} + \frac{1}{\frac{x^a+x^b}{x^a}} \quad 1$$

$$= \frac{x^b}{x^b+x^a} = \frac{x^a}{x^a+x^b} \quad 1$$

$$= \frac{(x^b+x^a)}{(x^a+x^b)} = 1. \quad 1$$

[CBSE Marking Scheme, 2012]

OR

$$\left(\frac{81}{16}\right)^{\frac{3}{4}} \times \left[\left(\frac{25}{9}\right)^{\frac{-3}{2}} + \left(\frac{5}{2}\right)^{-3}\right] = \left(\frac{3^4}{2^4}\right)^{\frac{3}{4}} \times \left[\left(\frac{5^2}{3^2}\right)^{\frac{-3}{2}} + \left(\frac{5}{2}\right)^{-3}\right] \quad 1$$

$$= \left(\frac{3}{2}\right)^{-3} \times \left[\left(\frac{5}{3}\right)^{-3} + \left(\frac{5}{2}\right)^{-3}\right] \quad 1$$

$$= \left(\frac{3}{2}\right)^{-3} \times \left[\left(\frac{3}{5}\right)^3 + \left(\frac{2}{5}\right)^3\right] \quad \frac{1}{2}$$

$$= \left(\frac{3}{2}\right)^{-3} \times \left[\left(\frac{3}{5}\right)^3 \times \left(\frac{5}{2}\right)^3\right] \quad \frac{1}{2}$$

$$= \left(\frac{3}{2}\right)^{-3} \times \left(\frac{3}{2}\right)^3 \quad \frac{1}{2}$$

$$= 1 \quad \frac{1}{2}$$

[CBSE Marking Scheme, 2012, 2013]

22.
$$LHS. = \frac{(2\sqrt{5} + \sqrt{3})^2 + (2\sqrt{5} - \sqrt{3})^2}{(2\sqrt{5} - \sqrt{3})(2\sqrt{5} + \sqrt{3})} \quad 1$$

$$= \frac{4 \times 5 + 3 + 2 \times 2\sqrt{5} \times \sqrt{3} + 4 \times 5 + 3 - 2 \times 2\sqrt{5} \times \sqrt{3}}{(2\sqrt{5})^2 - (\sqrt{3})^2} \quad 1$$

$$= \frac{20 + 3 + 4\sqrt{15} + 20 + 3 - 4\sqrt{15}}{20 - 3} \quad 1$$

$$= \frac{46}{17} = \frac{46}{17} + \sqrt{15} \times (0) \quad 1$$

$$\therefore \frac{46}{17} + \sqrt{15}(0) = a + \sqrt{15}b = RHS$$

Comparing both sides, we get

$$a = \frac{46}{17}, b = 0$$

1

[CBSE Marking Scheme, 2012]

23. Volume of cuboid = $8x^3 + 12x^2 - 2x - 3$
 $= 4x^2(2x + 3) - 1(2x + 3)$ ½
 $= (2x + 3)(4x^2 - 1)$ ½
 $= (2x + 3)(2x - 1)(2x + 1)$ ½
- The possible dimensions are : $(2x - 1)$, $(2x + 1)$ and $(2x + 3)$. ½
- Verification : For $x = 5$
Dimensions are : $(2 \times 5 - 1)$, $(2 \times 5 + 1)$ and $(2 \times 5 + 3)$ i.e., 9, 11, 13 units. ½
Volume = $9 \times 11 \times 13$
 $= 1287$ cubic units ½
Given volume = $8(5)^3 + 12(5)^2 - 2(5) - 3$ ½
 $= 1000 + 300 - 10 - 3$
 $= 1287$ cubic units. ½
24. (i) (I) Possible length and breadth of the rectangle are the factors of its given area,
Area = $25a^2 - 35a + 12$
 $= 25a^2 - 15a - 20a + 12$ ½
 $= 5a(5a - 3) - 4(5a - 3)$
 $= (5a - 4)(5a - 3)$
- So, possible length and breadth are $(5a - 3)$ and $(5a - 4)$ units, respectively. ½
- (II) Area = $35y^2 + 13y - 12$
 $= 35y^2 + 28y - 15y - 12$ ½
 $= 7y(5y + 4) - 3(5y + 4)$
 $= (7y - 3)(5y + 4)$ ½
- So, possible length and breadth are $(7y - 3)$ and $(5y + 4)$ units
- (ii) Factorisation of polynomials. 1
- (iii) Expression of one's desire and news is very necessary. 1
25.
$$\begin{array}{r} x^2 + x + 1 \\ x + 2 \overline{) x^3 + 3x^2 + 3x + 5} \\ \underline{x^3 + 2x^2} \\ + x^2 + 3x \\ \underline{ + x^2 + 2x} \\ + x + 5 \\ \underline{ + x + 2} \\ + 3 \end{array}$$
 1
- Hence, ½
and ½
Quotient = $x^2 + x + 1$
Remainder = 3.
26. (i) The co-ordinate of $B = (-2, 3)$ 1
(ii) E is the point which is identified by the co-ordinates $(-3, -2)$ 1
(iii) The co-ordinate of the point D is $(6, 2)$
 \therefore Abscissa is 6. 1
(iv) The co-ordinate of the point C is $(3, -1)$
 \therefore Ordinate is -1 . 1

27. (i) $\sqrt{\frac{\sqrt{2}-1}{\sqrt{2}+1}}$ is an irrational number

$$\begin{aligned}\sqrt{\frac{\sqrt{2}-1}{\sqrt{2}+1}} &= \sqrt{\frac{(\sqrt{2}-1)(\sqrt{2}-1)}{(\sqrt{2}+1)(\sqrt{2}-1)}} && \frac{1}{2} \\ &= \sqrt{\frac{(\sqrt{2}-1)^2}{2-1}} && \frac{1}{2} \\ &= \sqrt{\frac{(\sqrt{2}-1)^2}{1}} = \sqrt{2} - 1 && \frac{1}{2}\end{aligned}$$

which is a rational number.

Let, there is a number x such that x^3 is an irrational number but x^5 is a rational number.

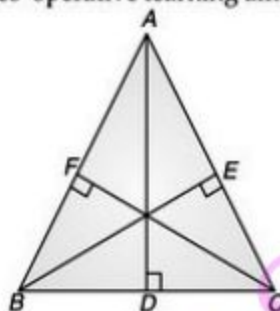
Let, $x = \sqrt[5]{7}$ is any number 1/2

$$x^3 = (\sqrt[5]{7})^3 = (7)^{3/5} \text{ is an irrational number} \quad \frac{1}{2}$$

But, $x^5 = (\sqrt[5]{7})^5 = (7)^{5/5} = 7$, is a rational number 1/2

(ii) Accepting own mistakes gracefully, co-operative learning among the classmates. 1

28.



Since from a point \perp^r line is the shortest.

$$\begin{aligned}CF &\perp AB \\ \therefore CF &< AC \text{ and } CF < BC && \dots(1) \quad 1\end{aligned}$$

Similarly, BC is a line segment and A does not lie on it. $AD \perp BC$

$$\therefore AD < AB \text{ and } AD < AC \quad \dots(2) \quad 1$$

Also, AC is a line segment and B does not lie on it. $BE \perp AC$

$$\therefore BE < AB \text{ and } BE < BC \quad \dots(3) \quad 1$$

Adding (1), (2) and (3), we get

$$2(AD + BE + CF) < 2(AB + BC + CA)$$

$$\therefore AB + BC + CA > AD + BE + CF \quad 1$$

i.e., Perimeter is greater than the sum of three altitudes. **Proved.**

OR

Produce AD to E such that, $AD = DE$. Join EC . 1

In triangles ADB and EDC , $AD = DE$ (Const) 1/2

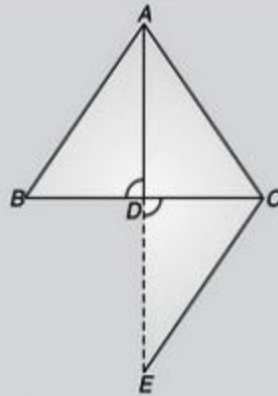
$BD = DC$ (Given)

$\angle ADB = \angle EDC$ (V.O.A) 1/2

$\therefore \Delta ADB \cong \Delta EDC$

(SAS congruence axiom) 1/2

$\Rightarrow AB = EC$ (By c.p.c.t.) 1/2



In $\triangle AEC$,
 \therefore

$$\begin{aligned} AC + EC &> AE \\ AC + AB &> AE \\ AC + AB &> AD + DE \\ AC + AB &> AD + AD \\ AC + AB &> 2AD. \end{aligned}$$

[Triangle Inequality Property] $\frac{1}{2}$

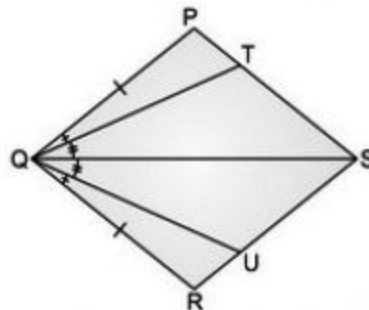
($\because EC = AB$)

($\because DE = AD$) $\frac{1}{2}$

Proved.

[CBSE Marking Scheme, 2012, 2013]

29.



\therefore
 \Rightarrow

$$\angle PQT = \angle RQU \text{ and } \angle TQS = \angle UQS$$

$$\angle PQT + \angle TQS = \angle RQU + \angle UQS$$

$$\angle PQS = \angle RQS$$

$$PQ = RQ,$$

$$QS = QS$$

$$\triangle PQS \cong \triangle RQS$$

$$\angle P = \angle R$$

\therefore
 \therefore

Again, in $\triangle PQT$ and $\triangle RQU$,

$$\angle P = \angle R$$

$$\angle PQT = \angle RQU$$

$$PQ = QR$$

$$\triangle PQT \cong \triangle RQU$$

$$QT = QU.$$

\therefore
 \therefore

1

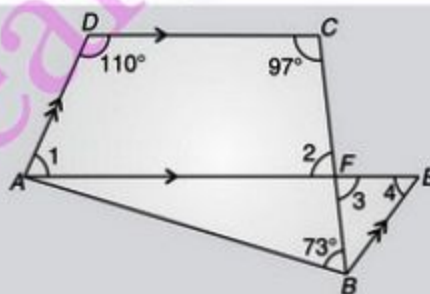
(By SAS) $\frac{1}{2}$

(By c.p.c.t.)

(By ASA) **1**

(By c.p.c.t.) $\frac{1}{2}$

30.



Since,

$$\begin{aligned} AE &\parallel DC \\ \angle D + \angle 1 &= 180^\circ \end{aligned}$$

(Angles on the same side of transversal)

	$\angle 1 = 180^\circ - 110^\circ = 70^\circ$	1
	$\angle 4 = \angle 1 = 70^\circ$	(Alternate angles) $\frac{1}{2}$
Again,	$97^\circ + \angle 2 = 180^\circ$	(Angle on the same side of transversal) $\frac{1}{2}$
	$\angle 2 = 180^\circ - 97^\circ = 83^\circ$	
	$\angle 3 = \angle 2 = 83^\circ$	(Vertically opp. angles) $\frac{1}{2}$
In $\triangle BEF$,	$\angle 3 + \angle 4 + \angle EBF = 180^\circ$	(Angle sum property) 1
	$83^\circ + 70^\circ + \angle EBF = 180^\circ$	
	$\angle EBF = 180^\circ - 153^\circ$	
	$\angle EBF = 27^\circ$	$\frac{1}{2}$
		[CBSE Marking Scheme, 2012]

31. (i) If a, b, c be the length of sides BC, CA and AB of $\triangle ABC$ and if $s = \frac{1}{2}(a + b + c)$ then,

\therefore Here, area of $\triangle ABC = \sqrt{s(s-a)(s-b)(s-c)}$

and $a = b = c (= a)$

$s = \frac{1}{2}(a + a + a) = \frac{3a}{2}$ $\frac{1}{2}$

$s - a = \frac{3a}{2} - a = \frac{a}{2}$

$s - b = \frac{3a}{2} - a = \frac{a}{2}$

$s - c = \frac{3a}{2} - a = \frac{a}{2}$ $\frac{1}{2}$

area = $\sqrt{\left(\frac{3a}{2}\right)\left(\frac{a}{2}\right)\left(\frac{a}{2}\right)\left(\frac{a}{2}\right)}$ $\frac{1}{2}$

$= \frac{a}{2} \times \frac{a}{2} \times \sqrt{3}$

$= \frac{\sqrt{3}a^2}{4}$ $\dots(1) \frac{1}{2}$

(ii) To find the area, when its perimeter = 180 cm^2

Here, $a + a + a = 180$

$\Rightarrow 3a = 180$ $\frac{1}{2}$

$\Rightarrow a = \frac{180}{3} = 60$

Hence, required area = $\frac{\sqrt{3}}{4} \times (60)^2$

$= 900\sqrt{3} \text{ cm}^2$ $\frac{1}{2}$

(iii) Heron's formula. $\frac{1}{2}$

(iv) We should follow the traffic rules to save our life. $\frac{1}{2}$



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