

SOLUTIONS

SAMPLE QUESTION PAPER - 2

Solved

Time : 3 Hours

Maximum Marks : 90

SECTION 'A'

1. (B) 2

1

2. (C) Number of zeroes of a cubic polynomial = 3

1

3. (B) Given :

$$x + \frac{1}{x} = 4$$

$$\left(x + \frac{1}{x}\right)^2 = x^2 + \frac{1}{x^2} + 2$$

$$(4)^2 = x^2 + \frac{1}{x^2} + 2$$

$$x^2 + \frac{1}{x^2} = 16 - 2 = 14$$

1

4. (C) For zeroes, put

$$p(x) = 0$$

$$2x + 7 = 0$$

$$x = \frac{-7}{2}$$

1

SECTION 'B'

5.

$$(4\sqrt{3} + 3\sqrt{2}) \times (4\sqrt{3} - 3\sqrt{2}) = (4\sqrt{3})^2 - (3\sqrt{2})^2$$

1

$$= 48 - 18$$

½

$$= 30.$$

½

[CBSE Marking Scheme, 2012, 2013]

6. Given,

$$p(x) = kx^2 - x - 4$$

$(x + 1)$ is a factor of $p(x)$, then

$$p(-1) = 0$$

½

$$k(-1)^2 - (-1) - 4 = 0$$

½

$$k + 1 - 4 = 0$$

½

$$k = 3$$

½

[CBSE Marking Scheme, 2012]

7.
$$\begin{aligned}x^2 - 9 &= (97)^2 - (3)^2 &\frac{1}{2} \\&= (97 + 3)(97 - 3) &\frac{1}{2} \\&= 100 \times 94 &\frac{1}{2} \\&= 9400. &\frac{1}{2}\end{aligned}$$

[CBSE Marking Scheme, 2012]

8. Euclid's axioms

- (i) Things which are equal to the same thing are equal to one another.
- (ii) If equals are added to equal, the wholes are equal.

1 + 1

[CBSE Marking Scheme, 2012, 2014]

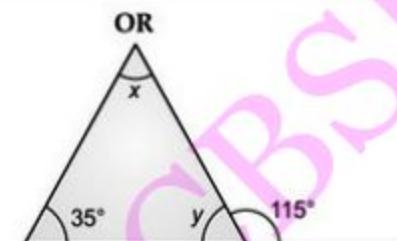
9.



$$\begin{aligned}x + y + z + w &= 360^\circ &1 \\(x + y) + (z + w) &= 360^\circ \\x + y + z + y &= 360^\circ &(\text{Since, } z + w = x + y) \frac{1}{2} \\2(x + y) &= 360^\circ \\x + y &= 180^\circ\end{aligned}$$

$\Rightarrow AOB$ is a straight line, as straight line makes an angle of 180° . $\frac{1}{2}$

[CBSE Marking Scheme, 2012]



$$\begin{aligned}x + 35^\circ &= 115^\circ \\x &= 115^\circ - 35^\circ = 80^\circ \\y &= 180^\circ - 115^\circ = 65^\circ &1\end{aligned}$$

10.

$$\begin{aligned}a &= 15 \text{ cm}, b = 15 \text{ cm}, c = 12 \text{ cm} \\s &= \frac{a+b+c}{2} = \frac{15+15+12}{2} = 21 \text{ cm} &\frac{1}{2} \\ \text{Area} &= \sqrt{s(s-a)(s-b)(s-c)} &\frac{1}{2} \\&= \sqrt{21 \times (21-15)(21-15)(21-12)} &\frac{1}{2} \\&= \sqrt{21 \times 6 \times 6 \times 9} \\&= 18\sqrt{21} \text{ cm}^2. &\frac{1}{2}\end{aligned}$$

[CBSE Marking Scheme, 2012]

SECTION 'C'

11.
$$\begin{aligned} \left(\frac{5^{-1} \times 7^2}{5^2 \times 7^{-4}}\right)^{\frac{7}{2}} \times \left(\frac{5^{-2} \times 7^3}{5^3 \times 7^{-5}}\right)^{\frac{5}{2}} &= \left(\frac{7^4 \times 7^2}{5^2 \times 5^1}\right)^{\frac{7}{2}} \times \left(\frac{7^5 \times 7^3}{5^3 \times 5^2}\right)^{\frac{5}{2}} \\ \Rightarrow &= \left(\frac{7^6}{5^3}\right)^{\frac{7}{2}} \times \left(\frac{7^8}{5^5}\right)^{\frac{5}{2}} \\ &= \frac{(7^6)^{7/2}}{(5^3)^{7/2}} \times \frac{(5^5)^{5/2}}{(7^8)^{5/2}} \\ \Rightarrow &= \frac{7^{21}}{5^{21/2}} \times \frac{5^{25/2}}{7^{20}} \\ &= 7^{21-20} \times (5)^{\left(\frac{25-21}{2}\right)} \\ &= 7^1 \times 5^2 \\ &= 7 \times 25 = 175 \end{aligned} \quad \frac{1}{2} \quad \frac{1}{2} \quad \frac{1}{2} \quad \frac{1}{2}$$

[CBSE Marking Scheme, 2012]

OR

$$\begin{aligned} \frac{\sqrt{6}}{\sqrt{2} + \sqrt{3}} &= \sqrt{18} - \sqrt{12} = 3\sqrt{2} - 2\sqrt{3} \\ \frac{3\sqrt{2}}{\sqrt{6} + \sqrt{3}} &= \sqrt{12} - \sqrt{6} = 2\sqrt{3} - \sqrt{6} \\ \frac{4\sqrt{3}}{\sqrt{6} + \sqrt{2}} &= \sqrt{18} - \sqrt{6} = 3\sqrt{2} - \sqrt{6} \\ \therefore \frac{\sqrt{6}}{\sqrt{2} + \sqrt{3}} + \frac{3\sqrt{2}}{\sqrt{6} + \sqrt{3}} - \frac{4\sqrt{3}}{\sqrt{6} + \sqrt{2}} &= 3\sqrt{2} - 2\sqrt{3} + 2\sqrt{3} - \sqrt{6} - 3\sqrt{2} + \sqrt{6} \\ &= 0 \end{aligned} \quad \frac{1}{2} \quad \frac{1}{2} \quad \frac{1}{2} \quad \frac{1}{2}$$

[CBSE Marking Scheme, 2012]

12.
$$\begin{aligned} x^{abc} &= (x^a)^{bc} & 1 \\ &= (y)^{bc} & 1 \\ &= (y^b)^c \\ &= (z)^c \\ &= x \\ x^{abc} &= x^1 & 1 \\ \Rightarrow abc &= 1 & 1 \end{aligned}$$

[CBSE Marking Scheme, 2012]

13.
$$\begin{aligned} \frac{\sqrt{2}}{\sqrt{5}+2} - \frac{2}{\sqrt{10}-2\sqrt{2}} + \frac{8}{\sqrt{2}} &= \frac{\sqrt{2}(\sqrt{5}-2)}{(\sqrt{5}+2)(\sqrt{5}-2)} - \frac{2(\sqrt{10}+2\sqrt{2})}{(\sqrt{10}-2\sqrt{2})(\sqrt{10}+2\sqrt{2})} + \frac{8\sqrt{2}}{(\sqrt{2})(\sqrt{2})} \\ &= \frac{\sqrt{10}-2\sqrt{2}}{5-4} - \frac{2\sqrt{10}+4\sqrt{2}}{10-8} + \frac{8\sqrt{2}}{2} \\ &= \sqrt{10} - 2\sqrt{2} - \sqrt{10} - 2\sqrt{2} + 4\sqrt{2} = 0 \end{aligned} \quad 1 \quad 1 \quad 1$$

OR

Given, $3x + 2y = 20, xy = \frac{11}{9}$

Raising to power three on both sides.

$$\begin{aligned} (3x + 2y)^3 &= 20^3 & \frac{1}{2} \\ 27x^3 + 8y^3 + 18xy(3x + 2y) &= 8000 & \frac{1}{2} \\ 27x^3 + 8y^3 + 18 \times \left(\frac{11}{9}\right) \times 20 &= 8000 & (\therefore 3x + 2y = 20) \left(\because xy = \frac{11}{9}\right) 1 \\ 27x^3 + 8y^3 &= 8000 - 440 & \frac{1}{2} \\ 27x^3 + 8y^3 &= 7560 & \frac{1}{2} \end{aligned}$$

14. $\frac{(a^2 - b^2)^3 + (b^2 - c^2)^3 + (c^2 - a^2)^3}{(a-b)^3 + (b-c)^3 + (c-a)^3}$

Both Numerator and Denominator are of the form $a^3 + b^3 + c^3$

We know that when $a + b + c = 0$
then $a^3 + b^3 + c^3 = 3abc$

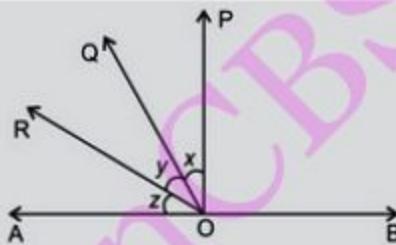
For Numerator, $a^2 - b^2 + b^2 - c^2 + c^2 - a^2 = 0$

For Denominator, $a - b + b - c + c - a = 0$

$$\begin{aligned} \therefore \frac{(a^2 - b^2)^3 + (b^2 - c^2)^3 + (c^2 - a^2)^3}{(a-b)^3 + (b-c)^3 + (c-a)^3} &= \frac{3 \times (a^2 - b^2)(b^2 - c^2)(c^2 - a^2)}{3(a-b)(b-c)(c-a)} & 1 \\ &= \frac{(a-b)(a+b)(b-c)(b+c)(c-a)(c+a)}{(a-b)(b-c)(c-a)} & \frac{1}{2} \\ &= (a+b)(b+c)(c+a). & \frac{1}{2} \end{aligned}$$

[CBSE Marking Scheme, 2012]

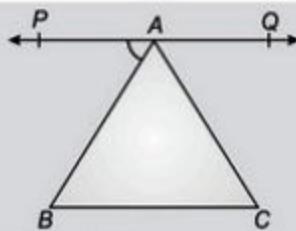
15.



$$\begin{aligned} \Rightarrow OP \perp AB & & \frac{1}{2} \\ \angle POA &= 90^\circ & \frac{1}{2} \\ \angle POQ &= a & \\ \angle QOR &= 3a & \\ \angle ROA &= 5a & \frac{1}{2} \\ \Rightarrow a + 3a + 5a &= 90^\circ & \frac{1}{2} \\ 9a &= 90^\circ & \frac{1}{2} \\ a &= 10^\circ & \\ \therefore x &= 10^\circ & \frac{1}{2} \\ y &= 3 \times 10^\circ = 30^\circ & \frac{1}{2} \\ z &= 5 \times 10^\circ = 50^\circ. & \frac{1}{2} \end{aligned}$$

[CBSE Marking Scheme, 2012, 2014] $\frac{1}{2}$

OR



Through vertex A,

 draw $PAQ \parallel BC$
 \therefore

$$\angle PAB = \angle ABC$$

 $\frac{1}{2}$
(Alternate angles)

$$\angle QAC = \angle ACB$$

 $\frac{1}{2}$
(Alternate angles)

 Adding above 2 equalities, $\angle PAB + \angle QAC = \angle ABC + \angle ACB$
 $\frac{1}{2}$

 Adding $\angle BAC$ to both sides, we get

 $\frac{1}{2}$

$$\angle PAB + \angle QAC + \angle BAC = \angle ABC + \angle ACB + \angle BAC$$

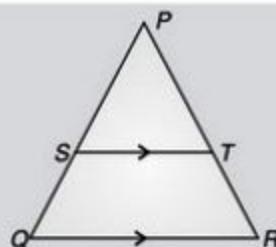
 \Rightarrow

$$180^\circ = \angle ABC + \angle ACB + \angle BAC.$$

 $\frac{1}{2}$
(Linear pair)

[CBSE Marking Scheme, 2012]

16.



$$PQ = PR \Rightarrow \angle PQR = \angle PRQ$$

 $\frac{1}{2}$
(Angles opp. to equal sides)

$$ST \parallel QR \Rightarrow \angle PST = \angle PQR$$

 $\frac{1}{2}$
(Corresponding angles)

$$\angle PTS = \angle PRQ$$

 $\frac{1}{2}$
(Corresponding angles)

 \therefore

$$\angle PST = \angle PTS$$

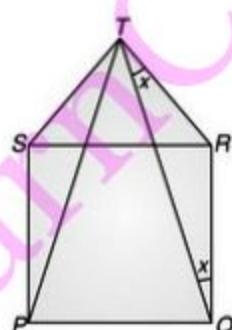
 $\frac{1}{2}$
 \Rightarrow

$$PS = PT.$$

 $\frac{1}{2}$
(Sides opp. to equal angles)

[CBSE Marking Scheme, 2012]

17. PQRS is a square.


 (i) $\triangle SRT$ is an equilateral triangle.

 \therefore

$$\angle PSR = 90^\circ, \angle TSR = 60^\circ$$

 $\frac{1}{2}$
 \Rightarrow

$$\angle PSR + \angle TSR = 150^\circ.$$

Similarly,

$$\angle QRT = 150^\circ$$

 $\triangle PST$ and $\triangle QRT$, we have

$$PS = QR (S)$$

 $\frac{1}{2}$

In

$$\angle PST = \angle QRT = 150^\circ (A) \text{ and } ST = RT (S)$$

By SAS,

$$\triangle PST \cong \triangle QRT$$

 $\frac{1}{2}$
 \Rightarrow

$$PT = QT$$

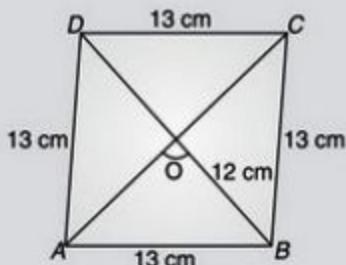
(By c.p.c.t.) Proved.

(ii) In $\triangle TQR$,

$$\begin{aligned} & QR = RT \quad (\text{Square and equilateral } \Delta \text{ on same base}) \frac{1}{2} \\ \Rightarrow & \angle TQR = \angle QTR = x \\ \therefore & x + x + \angle QRT = 180^\circ \\ & 2x + 150^\circ = 180^\circ \Rightarrow 2x = 30^\circ \\ \therefore & x = 15^\circ. \end{aligned}$$

Proved. 1

18. Rhombus,



$$\text{Perimeter} = 52 \text{ cm}$$

$$\text{Side} = \frac{52}{4} = 13 \text{ cm}$$

$$\text{Diagonal} = 24 \text{ cm}$$

$$OB = OD = 12 \text{ cm}$$

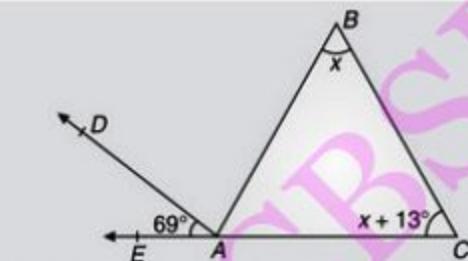
$$OA = \sqrt{13^2 - 12^2} = \sqrt{169 - 144} = \sqrt{25} = 5$$

$$\text{Area of rhombus} = 4 \times \frac{1}{2} \times 5 \times 12$$

$$\text{Area} = 120 \text{ cm}^2$$

[CBSE Marking Scheme, 2012]

19.



$$\angle EAD + \angle DAC = 180^\circ \quad (\text{Linear pair})$$

$$69^\circ + \angle DAC = 180^\circ$$

$$\angle DAC = 180^\circ - 69^\circ = 111^\circ$$

$$\angle CAB = y$$

$$\angle BAD = 2y$$

$$\text{Then, } y + 2y + 69 = 180 \quad (\text{Angle sum property of a triangle})$$

$$\Rightarrow 3y = 180 - 69 = 111$$

$$\Rightarrow y = 37^\circ$$

$$\angle CAB = y = 37$$

$$\angle BAD = 2y = 2 \times 37^\circ = 74^\circ$$

$$x + x + 13^\circ = 69^\circ + 74^\circ = 143^\circ \quad (\text{Exterior Angle})$$

$$2x = 130^\circ$$

$$x = 65^\circ$$

$$\angle C = x + 13^\circ = 65^\circ + 13^\circ = 78^\circ$$

$$\angle B = x = 65^\circ$$

$$\text{Thus, } \angle BAC = 37^\circ.$$

[CBSE Marking Scheme, 2012, 2014]

20. In the ΔQRT ,

$$\begin{aligned} 90^\circ + 40^\circ + x &= 180^\circ \\ x &= 180^\circ - 130^\circ = 50^\circ \end{aligned}$$

In the ΔPSR ,

\Rightarrow

and

$$\begin{aligned} \text{Ext } PSR &= y = x + 30^\circ \\ y &= 50^\circ + 30^\circ = 80^\circ \\ z &= 180^\circ - y \\ &= 180^\circ - 80^\circ = 100^\circ \end{aligned}$$

1
1
1
1

SECTION 'D'

21.

$$\begin{aligned} p(x) &= 2x^3 - 9x^2 + x + 12 \\ p(-1) &= 2(-1)^3 - 9(-1)^2 + (-1) + 12 \\ &= -2 - 9 - 1 + 12 \\ &= 0 \end{aligned}$$

$\Rightarrow x + 1$ is a factor of $f(x)$

$$\begin{aligned} p\left(\frac{3}{2}\right) &= 2\left(\frac{3}{2}\right)^3 - 9\left(\frac{3}{2}\right)^2 + \frac{3}{2} + 12 \\ &= 2\left(\frac{27}{8}\right) - 9\left(\frac{9}{4}\right) + \frac{3}{2} + 12 \\ &= \frac{27}{4} - \frac{81}{4} + \frac{3}{2} + 12 \\ &= \frac{27 - 81 + 6 + 48}{4} \\ &= 0 \end{aligned}$$

$\Rightarrow 2x - 3$ is a factor of $p(x)$

$$(x+1)(2x-3) = 2x^2 - x - 3.$$

$$(2x^3 - 9x^2 + x + 12) \div (2x^2 - x - 3) = x - 4$$

\Rightarrow Remaining factor is $x - 4$.

½
½
½
½
½
½
½
½
1
1
1

[CBSE Marking Scheme, 2013]

OR

Alternative Method :

Given,

$$a + b + c = 3x$$

or

$$3x - a - b - c = 0$$

\therefore

$$x - a + x - b + x - c = 0$$

\Rightarrow

$$(x-a)^3 + (x-b)^3 + (x-c)^3 = 3(x-a)(x-b)(x-c)$$

\Rightarrow

$$(x-a)^3 + (x-b)^3 + (x-c)^3 - 3(x-a)(x-b)(x-c)$$

$$= 3(x-a)(x-b)(x-c) - 3(x-a)(x-b)(x-c)$$

$$= 0.$$

1
1
1
1
1
1

22.

$$\frac{4}{(2187)^{\frac{3}{7}}} - \frac{5}{(256)^{\frac{1}{4}}} + \frac{2}{(1331^2)^{\frac{1}{3}}} = 4 \times (2187^{\frac{1}{7}})^3 - 5 \times 256^{1/4} + 2 \times (1331^{\frac{1}{3}})^2$$

1½

$$= 4 \times \left((3^7)^{\frac{1}{7}} \right)^3 - 5 \times (4^4)^{1/4} + 2 \times \left((11^3)^{\frac{1}{3}} \right)^2$$

1½

$$= 4 \times 27 - 5 \times 4 + 2 \times 121$$

$$= 108 - 20 + 242 = 330$$

1

[CBSE Marking Scheme, 2012]

23.

$$\begin{aligned}
 LHS &= 2x^3 + 2y^3 + 2z^3 - 6xyz \\
 &= 2(x^3 + y^3 + z^3 - 3xyz) \\
 &= 2[(x + y + z)(x^2 + y^2 + z^2 - xy - yz - zx)] \\
 &= [(x + y + z)(2x^2 + 2y^2 + 2z^2 - 2xy - 2yz - 2zx)] \\
 &= [(x + y + z)(x^2 - 2xy + y^2 + y^2 - 2yz + z^2 + z^2 - 2zx + x^2)] \\
 &= (x + y + z)[(x - y)^2 + (y - z)^2 + (z - x)^2] \\
 &= R.H.S
 \end{aligned}$$

Hence proved. $\frac{1}{2}$

$$\begin{aligned}
 2(13)^3 + 2(14)^3 + 2(15)^3 - 6 \times 13 \times 14 \times 15 \\
 &= (13 + 14 + 15)[(13 - 14)^2 + (14 - 15)^2 + (15 - 13)^2] \\
 &= 42 \times (1 + 1 + 4) \\
 &= 42 \times 6 = 252
 \end{aligned}$$

$\frac{1}{2}$

[CBSE Marking Scheme, 2013]

24. (i) $(998)^3 = (1000 - 2)^3$

We know that $(a - b)^3 = a^3 - b^3 - 3ab(a - b)$

Hence, $(998)^3 = (1000)^3 - (2)^3 - (3)(1000)(2)(1000 - 2)$

$$\begin{aligned}
 &= 1000000000 - 8 - 6000 \times 998 \\
 &= 1000000000 - 5988008 \\
 &= 994011992.
 \end{aligned}$$

(ii) Algebraic Identities $\frac{1}{2}$
 (iii) Satisfaction solves the identity crisis among people. $\frac{1}{2}$

25. $p(x) = ax^4 + 2x^3 - 3x^2 + bx - 4$
 $x^2 - 4$ or $(x - 2)(x + 2)$ is a factor of $p(x)$,
 then put $x = 2$ in $p(x) \Rightarrow p(2) = 0$

$$\begin{aligned}
 a(2)^4 + 2(2)^3 + 3(2)^2 + b \times 2 - 4 &= 0 \\
 16a + 16 - 12 + 2b - 4 &= 0 \\
 16a + 2b &= 0 \\
 8a + b &= 0
 \end{aligned}$$

... (1) $\frac{1}{2}$

Again put $x = -2$ in $p(x)$. $\Rightarrow p(-2) = 0$

$$\begin{aligned}
 a(-2)^4 + 2(-2)^3 - 3(-2)^2 + b \times (-2) - 4 &= 0 \\
 16a - 16 - 12 - 2b - 4 &= 0 \\
 16a - 2b &= 32 \\
 8a - b &= 16
 \end{aligned}$$

... (2) $\frac{1}{2}$

Adding eqs. (1) and (2), $16a = 16 \Rightarrow a = 1$ $\frac{1}{2}$

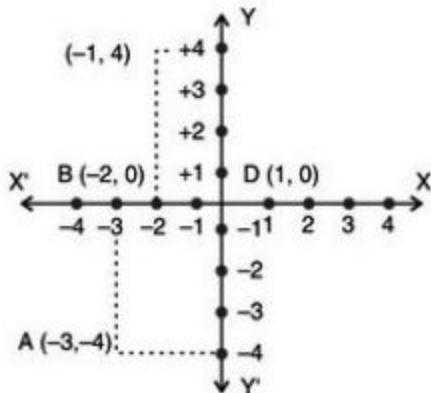
By equation (1), $8 \times 1 + b = 0 \Rightarrow b = -8$ $\frac{1}{2}$

$$\begin{aligned}
 p(x) &= x^4 + 2x^3 - 3x^2 - 8x - 4 \\
 &= (x^2 - 4)(x^2 + 2x + 1) \\
 &= (x - 2)(x + 2)(x + 1)^2.
 \end{aligned}$$

$\frac{1}{2}$

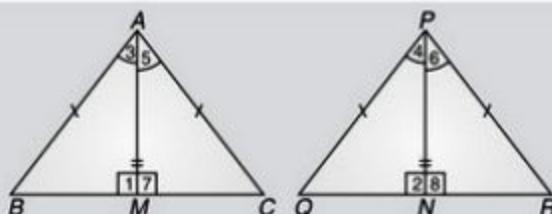
$$\begin{array}{r}
 x^2 + 2x + 1 \\
 x^2 - 4) \underline{x^4 + 2x^3 - 3x^2 - 8x - 4} \\
 \underline{x^4} \quad \underline{- 4x^2} \\
 \underline{\underline{2x^3 + x^2 - 8x - 4}} \\
 \underline{2x^3} \quad \underline{- 8x} \\
 \underline{\underline{- x^2 - 4}} \\
 \underline{\underline{- +}} \\
 \underline{\underline{0}}
 \end{array}$$

26.



- | | | |
|------------|-----------------------|---|
| A (-3, -4) | 3 rd quad. | 1 |
| B (-2, 0) | on X-axis | 1 |
| C (-1, 4) | 2 nd quad. | 1 |
| D (1, 0) | on X-axis | 1 |

27.


 In $\triangle AMB$ and $\triangle PNQ$,

$$\begin{aligned} AB &= PQ && \text{(Given)} \\ AM &= PN && \text{(Given)} \\ \angle 1 &= \angle 2 = 90^\circ && \end{aligned}$$

$$\begin{aligned} \Rightarrow \quad \triangle AMB &\cong \triangle PNQ && (\text{AM} \perp BC \& PN \perp QR) \\ \Rightarrow \quad \angle 3 &= \angle 4 && \text{(By RHS)} \\ \text{Similarly, } \quad \triangle AMC &\cong \triangle PNR && \text{(By c.p.c.t.) 2} \\ \Rightarrow \quad \angle 5 &= \angle 6 && \end{aligned}$$

(In congruent triangles, corresponding angles are equal)

 ∴ In $\triangle ABC$ and $\triangle PQR$,

$$\begin{aligned} AB &= PQ && \text{(Given)} \\ AC &= PR && \text{(Given)} \\ \angle A &= \angle P && \\ (\angle 3 + \angle 5 &= \angle 4 + \angle 6) && \text{(Proved)} \\ \Rightarrow \quad \triangle ABC &\cong \triangle PQR. && \text{(By SAS) 2} \end{aligned}$$

[CBSE Marking Scheme, 2012]

28.

$$\angle XAK + \angle KAH = 180^\circ \quad \text{(Linear pair)}$$

$$\angle KAH = 180^\circ - 137^\circ = 43^\circ \quad (\therefore \angle CAX = \angle XAK = 137^\circ, \text{ Given})$$

$$AB = AC \quad \text{(Given) 1}$$

$$\therefore \angle ABC = \angle ACB \quad \text{(Angles opp to equal sides are equal)}$$

$$\angle ABC + \angle ACB = 137^\circ, \quad \text{(ext. angle)}$$

$$\therefore \angle ABC = \angle ACB = \frac{137^\circ}{2} = 68.5^\circ \quad \frac{1}{2}$$

$$CH = CB \quad \text{(Given)}$$

$$\Rightarrow \angle CBA = \angle CHB = 68.5^\circ \quad \frac{1}{2}$$

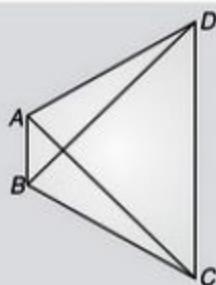
$$\therefore \angle HCB = 180^\circ - 137^\circ = 43^\circ$$

$$\angle CHK = \angle HCB = 43^\circ.$$

(Alternate angles) 1

[CBSE Marking Scheme, 2012, 2013]

OR



Proof : In $\triangle ABC$,

$$BC > AB \quad (\because AB \text{ smallest side})$$

$$\angle BAC > \angle ACB \quad \dots(i)$$

In $\triangle ACD$,

$$CD > AD \quad (\because CD \text{ greatest side}) \frac{1}{2}$$

$$\angle CAD > \angle ACD \quad \dots(ii)$$

Adding (i) and (ii), we get

$$\angle BAC + \angle CAD > \angle ACB + \angle ACD \quad \frac{1}{2}$$

\Rightarrow

$$\angle BAD > \angle BCD$$

$$\angle A > \angle C \quad 1$$

In $\triangle ABD$,

$$AD > AB \quad \dots(iii) \frac{1}{2}$$

\therefore

$$\angle ABD > \angle ADB \quad \dots(iv) \frac{1}{2}$$

In $\triangle BCD$,

$$CD > BC \quad \dots(iv) \frac{1}{2}$$

\therefore

$$\angle CBD > \angle BDC \quad \dots(iv) \frac{1}{2}$$

Adding (iii) and (iv), we get

$$\angle ABD + \angle CBD > \angle ADB + \angle BDC$$

$$\angle ABC > \angle ADC$$

$$\angle B > \angle D \quad 1$$

Hence, $\angle A > \angle C$ and $\angle B > \angle D$.

[CBSE Marking Scheme, 2012]

29. By triangle inequality property,

In $\triangle ABC$,

$$AB + BC > AC$$

In $\triangle ABCD$,

$$BC + CD > BD$$

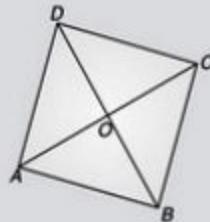
In $\triangle ACDA$,

$$CD + DA > AC$$

In $\triangle DAB$,

$$DA + AB > BD$$

Using the fact that sum of two sides of a triangle is greater than the third side



...(1) $\frac{1}{2}$

...(2) $\frac{1}{2}$

...(3) $\frac{1}{2}$

...(4) $\frac{1}{2}$

Adding (1), (2), (3) and (4), we get

$$AB + BC + BC + CD + CD + DA + DA + AB > AC + BD + AC + BD \quad 1$$

$$2(AB + BC + CD + DA) > 2(AC + BD)$$

Hence,

$$\text{Perimeter} > \text{Sum of its diagonals.} \quad 1$$

[CBSE Marking Scheme, 2012, 2013]

30.

$$\angle AGH = \angle GHD$$

$\frac{1}{2}$

\Rightarrow

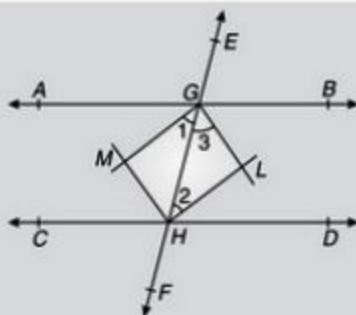
$$\frac{1}{2} \angle AGH = \frac{1}{2} \angle GHD \Rightarrow \angle 1 = \angle 2$$

\Rightarrow

Similarly,

$$GM \parallel LH$$

$$GL \parallel MH$$



$\Rightarrow GMHL$ is a parallelogram

1

$$\angle BGH + \angle GHD = 180^\circ$$

$$\Rightarrow \frac{1}{2} \angle BGH + \frac{1}{2} (\angle GHD) = 90^\circ$$

½

$$\Rightarrow \angle 3 + \angle 2 = 90^\circ$$

In $\triangle GLH$,

1

$$\angle GLH = 180^\circ - (\angle 2 + \angle 3)$$

$$= 180^\circ - 90^\circ$$

$$\Rightarrow \angle GLH = 90^\circ$$

1

$$\Rightarrow \angle GMH = 90^\circ$$

So,

$$\angle MGL + \angle GLH = 180^\circ \Rightarrow \angle MGL + 90^\circ$$

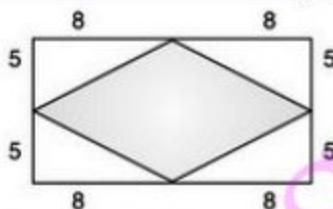
$$= 180^\circ$$

$$\Rightarrow \angle MGL = 90^\circ \Rightarrow \angle MHL = 90^\circ.$$

1

[CBSE Marking Scheme, 2012, 2013]

31.



$$\text{Area of rectangle} = 16 \times 10 \\ = 160 \text{ sq. units}$$

Four right angled triangles are cut from the paper to form the rhombus.

$$\text{Area of each triangle} = \frac{1}{2} \times 8 \times 5 \\ = 20 \text{ sq units}$$

1

Hence, area of four triangles = 80 sq. units.

$$\text{Hence, area of the rhombus} = 160 - 80 \\ = 80 \text{ sq. units}$$

1

Now the area of the base triangle with sides 5, 6, 5 units

$$s = \frac{5+6+5}{2} \\ = 8$$

1

By Heron's formula,

$$\text{Area} = \sqrt{s(s-a)(s-b)(s-c)} \\ = \sqrt{8(8-5)(8-6)(8-5)} \\ = \sqrt{8 \times 3 \times 2 \times 3} \\ = 12$$

1

Therefore the area of the kite is $80 + 12 = 92$ sq. units.

1



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