

SOLUTIONS

SAMPLE QUESTION PAPER - 5

Solved _____

Time : 3 Hours

Maximum Marks : 90

SECTION 'A'

1. (C) $(81)^{-1/4} \times \sqrt[3]{81} = (3^4)^{-1/4} \times (3^4)^{1/4}$ 1
 $= (3)^{-1} \times (3)^1$
 $= (3)^{-1+1} = 3^0 = 1$
2. (C) $\frac{x}{y} + \frac{y}{x} = -1$
 $\frac{x^2 + y^2}{xy} = -1$
 $x^2 + y^2 = -xy$
 $x^2 + y^2 + xy = 0$
 $x^3 - y^3 = (x - y)(x^2 + y^2 + xy) = (x - y) \times 0 = 0$ 1
3. (C) $p(x) = 3x^3 - 2x^2 - x + 4$
 $p(-1) = 3(-1)^3 - 2(-1)^2 - (-1) + 4$
 $= -3 - 2 + 1 + 4$
 $= 0.$ 1
4. (B) (5, 0) 1

SECTION 'B'

5. $\sqrt{50} - \sqrt{98} + \sqrt{162}$
 $= \sqrt{5 \times 5 \times 2} - \sqrt{7 \times 7 \times 2} + \sqrt{3 \times 3 \times 3 \times 2}$ 1
 $= 5\sqrt{2} - 7\sqrt{2} + 9\sqrt{2}$ ½
 $= 7\sqrt{2}$ ½

[CBSE Marking Scheme, 2012]

6. $\left(x + \frac{1}{x}\right) \left(x - \frac{1}{x}\right) \left(x^2 + \frac{1}{x^2}\right) \left(x^4 + \frac{1}{x^4}\right) = \left(x^2 - \frac{1}{x^2}\right) \left(x^2 + \frac{1}{x^2}\right) \left(x^4 + \frac{1}{x^4}\right)$ ½
 as $(a + b)(a - b) = a^2 - b^2$ ½

$$= \left(x^4 - \frac{1}{x^4}\right) \left(x^4 + \frac{1}{x^4}\right) \quad \frac{1}{2}$$

$$= \left(x^8 - \frac{1}{x^8}\right) \quad \frac{1}{2}$$

[CBSE Marking Scheme, 2011, 2012]

7. $m(m-1) - n(n-1) = m^2 - m - n^2 + n \quad \frac{1}{2}$
 $= m^2 - n^2 - m + n$
 $= (m-n)(m+n) - (m-n) \quad 1$
 $= (m-n)(m+n-1) \quad \frac{1}{2}$

[CBSE Marking Scheme, 2012]

8. $AB = CD \quad (\text{Given})$
 $AB + BC = BC + CD \quad \frac{1}{2} + \frac{1}{2}$
 $AC = BD$

Euclid's axiom used : If equals are added to equals, the wholes are equal. 1

[CBSE Marking Scheme, 2012, 2014]

9. $a + b = 180^\circ \quad (\text{Linear pair}) \quad \frac{1}{2}$
 $a - b = 80^\circ \quad (\text{Given})$
 Adding, $2a = 260^\circ \quad \frac{1}{2}$
 $a = 130^\circ \quad \frac{1}{2}$
 $b = 180^\circ - a = 180^\circ - 130^\circ$
 $= 50^\circ. \quad \frac{1}{2}$

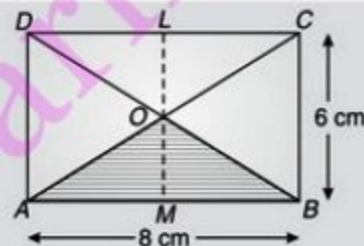
[CBSE Marking Scheme, 2010, 2011, 2012]

OR

Let, $\angle a = 2x$ and $\angle b = 3x \quad \frac{1}{2}$
 Then, $\angle a + \angle b = 90^\circ$
 $2x + 3x = 90^\circ$
 $x = 18^\circ \quad \frac{1}{2}$
 $a = 2 \times 18^\circ = 36^\circ$
 $b = 3 \times 18^\circ = 54^\circ$
 $\therefore c = 180^\circ - b = 180^\circ - 54^\circ$
 $= 126^\circ. \quad 1$

[CBSE Marking Scheme, 2012]

10.

Diagonals bisect each other at O
Draw, $LO \perp AB$ and CD

$$OL = OM = 3 \text{ cm} \quad 1$$

Area of shaded region

$$OAB = \frac{1}{2} \times 8 \times 3$$

$$= 12 \text{ cm}^2. \quad 1$$

[CBSE Marking Scheme, 2012]

SECTION 'C'

11.
$$\left[5^2(8^{1/3} + 27^{1/3})^3\right]^{1/5} = \left[5^2\left\{(2^3)^{1/3} + (3^3)^{1/3}\right\}^3\right]^{1/5} \quad 1$$

$$= [25(2+3)^3]^{1/5}$$

$$= [5^2 \times 5^3]^{1/5} \quad 1$$

$$= (5^5)^{1/5}$$

$$= 5 \quad 1$$

OR

$$LHS = \frac{1}{3-\sqrt{8}} - \frac{1}{\sqrt{8}-\sqrt{7}} + \frac{1}{\sqrt{7}-\sqrt{6}} - \frac{1}{\sqrt{6}-\sqrt{5}} + \frac{1}{\sqrt{5}-2}$$

$$= \frac{1}{(3-\sqrt{8})} \times \frac{(3+\sqrt{8})}{(3+\sqrt{8})} - \frac{1}{(\sqrt{8}-\sqrt{7})} \times \frac{(\sqrt{8}+\sqrt{7})}{(\sqrt{8}+\sqrt{7})} + \frac{1}{(\sqrt{7}-\sqrt{6})} \times \frac{(\sqrt{7}+\sqrt{6})}{(\sqrt{7}+\sqrt{6})} - \frac{1}{(\sqrt{6}-\sqrt{5})} \times \frac{(\sqrt{6}+\sqrt{5})}{(\sqrt{6}+\sqrt{5})}$$

$$+ \frac{1}{\sqrt{5}-2} \times \frac{\sqrt{5}+2}{\sqrt{5}+2} \quad 1$$

$$= \frac{(3+\sqrt{8})}{9-8} - \frac{(\sqrt{8}+\sqrt{7})}{8-7} + \frac{(\sqrt{7}+\sqrt{6})}{7-6} - \frac{(\sqrt{6}+\sqrt{5})}{6-5} + \frac{(\sqrt{5}+2)}{5-4}$$

$$= (3+\sqrt{8}) - (\sqrt{8}+\sqrt{7}) + (\sqrt{7}+\sqrt{6}) - (\sqrt{6}+\sqrt{5}) + \sqrt{5}+2$$

$$= 3+\sqrt{8} - \sqrt{8}-\sqrt{7} + \sqrt{7}+\sqrt{6} - \sqrt{6}-\sqrt{5} + \sqrt{5}+2 \quad 1$$

$$= 3+2 \quad 1$$

$$= 5$$

$$= RHS$$

12. Given,
then,

$$x + y = 5$$

$$x^3 + y^3 + 15xy - 125 = x^3 + y^3 - 125 + 15xy$$

$$= x^3 + y^3 + (-5)^3 - 3xy(-5) \quad 1/2$$

$$= (x + y - 5) [(x)^2 + (y)^2 + (-5)^2 - x(-5) - y(-5) - xy] \quad 1$$

$$= (5 - 5) (x^2 + y^2 + 25 + 5x + 5y - xy) \quad (\because x + y = 5) \quad 1/2$$

$$= 0 (x^2 + y^2 + 25 + 5x + 5y - xy) \quad 1/2$$

$$= 0 \quad 1/2$$

13. $125x^3 - 27y^3 + z^3 + 45xyz = (5x)^3 + (-3y)^3 + (z)^3 - 3 \times (5x) \times (-3y) \times (z)$ 1

$$= (5x - 3y + z) [(5x)^2 + (-3y)^2 + (z)^2 - (5x)(-3y) - (-3y)(z) - (5x)(z)] \quad 1$$

$$= (5x - 3y + z) [25x^2 + 9y^2 + z^2 + 15xy + 3yz - 5xz] \quad 1$$

[CBSE Marking Scheme, 2012]

OR

Let, $p(x) = x^6 - ax^5 + x^4 - ax^3 + 3x - a + 2$

$(x - a)$ is a factor of the polynomial $p(x)$, then

$$p(a) = 0 \quad 1$$

$$a^6 - a \times a^5 + a^4 - a \times a^3 + 3 \times a - a + 2 = 0 \quad 1$$

$$a^6 - a^6 + a^4 - a^4 + 3a - a + 2 = 0 \quad 1/2$$

$$2a = -2 \Rightarrow a = -1. \quad 1/2$$

$$\begin{aligned}
 14. \quad \frac{3}{4\sqrt{5}-\sqrt{3}} + \frac{2}{4\sqrt{5}+\sqrt{3}} &= \frac{3(4\sqrt{5}+\sqrt{3})+2(4\sqrt{5}-\sqrt{3})}{(4\sqrt{5})^2-(\sqrt{3})^2} && \frac{1}{2} \\
 &= \frac{12\sqrt{5}+3\sqrt{3}+8\sqrt{5}-2\sqrt{3}}{80-3} && 1 \\
 &= \frac{20\sqrt{5}+\sqrt{3}}{77} && \frac{1}{2} \\
 \text{On comparing we get,} & \quad a = \frac{20}{77} \text{ and } b = \frac{1}{77} && 1
 \end{aligned}$$

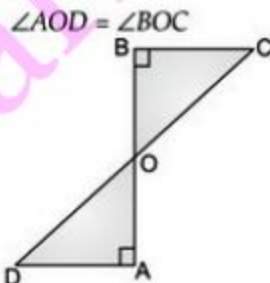
15. Given,	$\angle POR : \angle ROQ = 5 : 7$	
Let,	$\angle POR = 5x$	$\frac{1}{2}$
and	$\angle ROQ = 7x$	$\frac{1}{2}$
\Rightarrow	$5x + 7x = 180^\circ$	
\Rightarrow	$12x = 180^\circ$	
	$x = \frac{180}{12} = 15^\circ$	1
	$\angle POR = d = b = 5x = 5 \times 15^\circ = 75^\circ$	
	$\angle ROQ = c = a = 7x = 7 \times 15^\circ = 105^\circ.$	1

[CBSE Marking Scheme, 2012]

OR

$$\begin{aligned}
 x + 9^\circ + 5\left(\frac{x}{2} - 1^\circ\right) + \frac{1}{2}x &= 180^\circ && \text{(Linear pair) } 1 \\
 x + 9^\circ + \frac{5x}{2} - 5^\circ + \frac{1}{2}x &= 180^\circ \\
 4x &= 176^\circ && 1 \\
 x &= 44^\circ \\
 a + b &= \frac{1}{2}x^\circ + 5\left(\frac{x^\circ}{2} - 1^\circ\right) && \text{(Exterior angle)} \\
 &= \frac{1}{2}x^\circ + \frac{5x^\circ}{2} - 5^\circ \\
 &= 3x^\circ - 5^\circ \\
 &= 3 \times 44^\circ - 5^\circ \\
 &= 132^\circ - 5^\circ = 127^\circ. && 1
 \end{aligned}$$

[CBSE Marking Scheme, 2012]

16. (i) AB and CD intersect at O . \therefore  $\angle AOD = \angle BOC$ (Vertically opp. angles) ... (i) $\frac{1}{2}$ In $\triangle AOD$ and $\triangle BOC$, we have

$$\begin{aligned}
 \angle AOD &= \angle BOC \\
 \angle DAO &= \angle CBO = 90^\circ
 \end{aligned}$$

$\frac{1}{2}$
[From (i)]
(Given) $\frac{1}{2}$

and $AD = BC$ (Given)
 $\therefore \Delta AOD \cong \Delta BOC$ (By AAS congruence criterion)
 $\Rightarrow OA = OB$ (By c.p.c.t.)
i.e. O is the mid-point of AB .
Hence, CD bisects AB . 1/2

- (ii) Congruence of triangles. 1/2
(iii) Equality is the sign of democracy. 1/2

17. In ΔABD and ΔCDB ,



$AB = CD$ (Given) 1
 $\angle ABD = \angle CDB$ (Given)
 $BD = BD$ (Common) 1
 $\therefore \Delta ABD \cong \Delta CDB$ (By SAS)
 $\Rightarrow AD = CB$. (By c.p.c.t.) 1

[CBSE Marking Scheme, 2012]

18. Semi-perimeter of ΔABC ,

$$s = \frac{34 + 20 + 42}{2}$$

$$= \frac{96}{2} = 48 \text{ cm}$$

$$\text{Area of } \Delta ABC = \sqrt{s(s-a)(s-b)(s-c)} \quad 1/2$$

$$= \sqrt{48 \times 14 \times 28 \times 16}$$

$$= 6 \times 8 \times 7 = 336 \text{ cm}^2 \quad 1$$

Area of Parallelogram $= 2 \times \text{Area of } \Delta ABC$ 1/2

$$= 2 \times 336 = 672 \text{ cm}^2 \quad 1$$

[CBSE Marking Scheme, 2012]

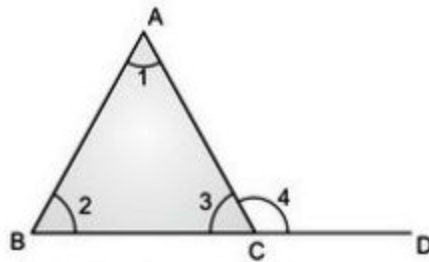
19. $ABCD$ is a rectangle.

$\Rightarrow AB = DC$ and $AD = BC$
 E bisects $BC \Rightarrow BE = EC$ 1



In ΔECD and EBA ,
 $DC = AB$
 $EC = BE$
 $\angle DCE = \angle ABE = 90^\circ$
 $\therefore \Delta ECD \cong \Delta EBA$ (By SAS) 1
 $\Rightarrow AE = DE$ (By c.p.c.t.) 1

20. **Proof :** In ΔABC , $\angle 1 + \angle 2 + \angle 3 = 180^\circ$ (Asp.) ... (i) 1
and $\angle 3 + \angle 4 = 180^\circ$ (lp.) ... (ii) 1
From equations (i) and (ii)



⇒
Hence,

$$\begin{aligned}\angle 1 + \angle 2 + \angle 3 &= \angle 3 + \angle 4 \\ \angle 4 &= \angle 1 + \angle 2 \\ \angle A + \angle B &= \angle ACD\end{aligned}$$

1

SECTION 'D'

21.

$$a\sqrt{5} - \frac{b}{11} = \frac{(3-\sqrt{5})(3-2\sqrt{5})}{(3+2\sqrt{5})(3-2\sqrt{5})} \quad \frac{1}{2}$$

$$= \frac{9-6\sqrt{5}-3\sqrt{5}+2 \times 5}{(3)^2 - (2\sqrt{5})^2} \quad 1$$

$$= \frac{9-9\sqrt{5}+10}{9-20} \quad \frac{1}{2}$$

$$= \frac{19-9\sqrt{5}}{-11} \quad \frac{1}{2}$$

$$= \frac{19}{-11} - \frac{9\sqrt{5}}{-11} = \frac{9\sqrt{5}}{11} - \frac{19}{11} \quad \frac{1}{2}$$

$$a\sqrt{5} - \frac{b}{11} = \frac{-19}{11} + \frac{9\sqrt{5}}{11}$$

⇒

$$a\sqrt{5} - \frac{b}{11} = \frac{9}{11}\sqrt{5} - \frac{19}{11} \quad \frac{1}{2}$$

On comparing both sides, we get

$$a = \frac{9}{11}, b = 19. \quad \frac{1}{2}$$

[CBSE Marking Scheme, 2012]

OR

(i) We know that between two rational numbers x and y , such that $x < y$ there is a rational number

$$\frac{x+y}{2}.$$

i.e., $3 < \frac{7}{2} < 4$ $\frac{1}{2}$

Now, a rational number between 3 and $\frac{7}{2} < 4$ is :

$$\frac{1}{2}\left(3 + \frac{7}{2}\right) = \frac{1}{2} \times \left(\frac{6+7}{2}\right) = \frac{13}{4} \quad \frac{1}{2}$$

A rational number between $\frac{7}{2}$ and 4 is :

$$\frac{1}{2}\left(\frac{7}{2}+4\right) = \frac{1}{2} \times \left(\frac{7+8}{2}\right) = \frac{15}{4}$$

$$\therefore 3 < \frac{13}{4} < \frac{7}{2} < \frac{15}{4} < 4 \quad \frac{1}{2}$$

Further a rational number between 3 and $\frac{13}{4}$ is :

$$\frac{1}{2}\left(3 + \frac{13}{4}\right) = \frac{1}{2} \times \left(\frac{12+13}{4}\right) = \frac{25}{8}$$

A rational number between $\frac{15}{4}$ and 4 is :

$$\frac{1}{2}\left(\frac{15}{4} + 4\right) = \frac{1}{2} \times \frac{15+16}{4} = \frac{31}{8} \quad \frac{1}{2}$$

A rational number between $\frac{31}{8}$ and 4 is :

$$\frac{1}{2}\left(\frac{31}{8} + 4\right) = \frac{1}{2} \times \left(\frac{31+32}{8}\right) = \frac{63}{16} \quad \frac{1}{2}$$

$$\therefore 3 < \frac{25}{8} < \frac{13}{4} < \frac{7}{2} < \frac{15}{4} < \frac{13}{8} < \frac{63}{16} < 4$$

Hence, six rational numbers between 3 and 4 are :

$$\frac{25}{8}, \frac{13}{4}, \frac{7}{2}, \frac{15}{4}, \frac{31}{8} \text{ and } \frac{63}{16} \quad \frac{1}{2}$$

(ii) Number system. 1/2

(iii) Rationality is always welcomed. 1/2

22.
$$\left(\frac{x^a}{x^b}\right)^{\frac{1}{ab}} \times \left(\frac{x^b}{x^c}\right)^{\frac{1}{bc}} \times \left(\frac{x^c}{x^a}\right)^{\frac{1}{ca}} = \left(x^{a-b}\right)^{\frac{1}{ab}} \times \left(x^{b-c}\right)^{\frac{1}{bc}} \times \left(x^{c-a}\right)^{\frac{1}{ca}} \quad 1$$

$$= x^{\frac{a-b}{ab} + \frac{b-c}{bc} + \frac{c-a}{ca}} \quad \frac{1}{2}$$

$$= x^{\frac{a-b}{ab} + \frac{b-c}{bc} + \frac{c-a}{ca}} \quad \frac{1}{2}$$

$$= x^{\frac{ac-bc+ab-ca+bc-ab}{abc}} \quad 1$$

$$= x^{\frac{0}{abc}} = x^0 \quad \frac{1}{2}$$

$$= 1 \quad \frac{1}{2}$$

[CBSE Marking Scheme, 2012]

23. Let, $a^2 - 2a = x$ 1/2

$$x^2 - 23x + 120 = (x - 15)(x - 8) \quad 1$$

$$= (a^2 - 2a - 15)(a^2 - 2a - 8)$$

Now, $a^2 - 2a - 15 = (a - 5)(a + 3)$ 1

$$a^2 - 2a - 8 = (a - 4)(a + 2) \quad 1$$

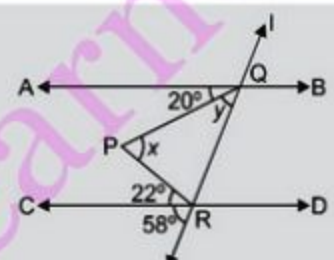
$$(a^2 - 2a)^2 - 23(a^2 - 2a) + 120 = (a - 5)(a + 3)(a - 4)(a + 2) \quad \frac{1}{2}$$

[CBSE Marking Scheme, 2012]

24. $f(x) = x^4 - 2x^3 + 3x^2 - 9x + 3a - 7$
 Put $x + 1 = 0$ or $x = -1$ in $f(x)$, we get
 $f(-1) = 20$
 $\Rightarrow (-1)^4 - 2(-1)^3 + 3(-1)^2 - 9(-1) + 3a - 7 = 20$ 1
 $\Rightarrow 1 + 2 + 3 + 9 + 3a - 7 = 20$
 $\therefore 3a = 20 - 8 \Rightarrow 3a = 12$
 $a = 4$ 1
 Again put, $x + 2 = 0$ or $x = -2$ in $f(x)$, we get
 Remainder = $f(-2)$
 $= (-2)^4 - 2(-2)^3 + 3(-2)^2 - 9(-2) + 3 \times (4) - 7$ 1
 $= 16 + 16 + 12 + 18 + 12 - 7$
 $= 74 - 7 = 67.$ 1
 [CBSE Marking Scheme, 2012]

25. $RHS = (x - y)(x^2 + xy + y^2)$
 $= x^3 + x^2y + xy^2 - x^2y - xy^2 - y^3$ 2
 $= x^3 - y^3 = LHS$
 $216x^3 - 125y^3 = (6x)^3 - (5y)^3$ 1
 $= (6x - 5y)[(6x)^2 + (5y)^2 + (6x)(5y)]$
 $= (6x - 5y)[36x^2 + 25y^2 + 30xy]$ 1

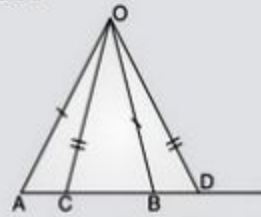
26. Let, $p(x) = x^2 + px + q$
 and $q(x) = x^2 + mx + n$
 Since $x + a$ is a factor of $p(x)$ and $q(x)$, then
 $p(-a) = 0$ and $q(-a) = 0$
 $p(-a) = 0 \Rightarrow (-a)^2 + p(-a) + q = 0$
 $a^2 - pa + q = 0$... (1) 1
 $q(-a) = 0 \Rightarrow (-a)^2 + m(-a) + n = 0$
 $a^2 - ma + n = 0$... (2) 1
 Subtracting eqn. (2) from eqn. (1), we get
 $a^2 - pa + q - a^2 + ma - n = 0$ 1
 $\Rightarrow a(m - p) = n - q$
 $\Rightarrow a = \frac{n - q}{m - p}$ [CBSE Marking Scheme, 2012] 1

27. 
 $y + 20^\circ = 58^\circ$ (Corr. angles)
 $\Rightarrow y = 58^\circ - 20^\circ = 38^\circ$ 1½
 $\angle PRQ = 180^\circ - (58^\circ + 22^\circ)$ (Linear pair)
 $= 180^\circ - 80^\circ = 100^\circ$ 1½
 $x = 180^\circ - (100^\circ + 38^\circ)$ (Angle sum property)
 $= 180^\circ - 138^\circ = 42^\circ.$ [CBSE Marking Scheme, 2012] 1

28.

In $\triangle AOC$ and $\triangle BOD$, \therefore

$$\begin{aligned} \angle AOB &= \angle COD && \text{(Given)} \\ \angle AOB - \angle COB &= \angle COD - \angle COB && \frac{1}{2} \\ \angle AOC &= \angle BOD && \frac{1}{2} \\ AO &= OB && \text{(Given)} \frac{1}{2} \\ OC &= OD && \text{(Given)} \\ \angle AOC &= \angle BOD && \text{(Proved above)} \frac{1}{2} \\ \triangle AOC &\cong \triangle BOD && \text{(SAS)} \mathbf{1} \\ AC &= BD. && \text{(By c.p.c.t.)} \mathbf{1} \end{aligned}$$



[CBSE Marking Scheme, 2012]

OR

As $\angle ABC$ and $\angle CBE$ form a linear pair.

$$\therefore \angle ABC + \angle CBE = 180^\circ$$

 $\therefore BO$ is the bisector of $\angle CBE$.

$$\angle CBE = 2 \angle 1$$

Therefore,

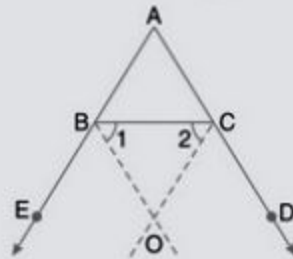
$$\angle ABC + 2 \angle 1 = 180^\circ$$

 \Rightarrow

$$2 \angle 1 = 180^\circ - \angle ABC$$

 \Rightarrow

$$\angle 1 = 90^\circ - \frac{1}{2} \angle ABC$$

... (i) $\frac{1}{2}$ Again, $\angle ACB$ and $\angle BCD$ form a linear pair.

$$\therefore \angle ACB + \angle BCD = 180^\circ$$

As CO is the bisector of $\angle BCD$, therefore

$$\angle BCD = 2 \angle 2$$

 \therefore

$$\angle ACB + 2 \angle 2 = 180^\circ$$

 \Rightarrow

$$2 \angle 2 = 180^\circ - \angle ACB$$

 \Rightarrow

$$\angle 2 = 90^\circ - \frac{1}{2} \angle ACB$$

... (ii) $\frac{1}{2}$ In $\triangle OBC$, we have $\angle 1 + \angle 2 + \angle BOC = 180^\circ$... (iii) $\frac{1}{2}$

From Eqn. (i), (ii) and (iii), we have

$$90^\circ - \frac{1}{2} \angle ABC + 90^\circ - \frac{1}{2} \angle ACB + \angle BOC = 180^\circ$$

... (iv) $\frac{1}{2}$ Now, in $\triangle ABC$, we have $\angle A + \angle B + \angle C = 180^\circ$ \Rightarrow

$$\angle B + \angle C = 180^\circ - \angle A$$

... (v) $\frac{1}{2}$

From Eqn. (iv) and (v), we have

$$180^\circ - \frac{1}{2} (180^\circ - \angle A) + \angle BOC = 180^\circ$$

 \Rightarrow

$$\angle BOC = 180^\circ - 180^\circ + \frac{1}{2} (180^\circ - \angle A)$$

 $\frac{1}{2}$ \Rightarrow

$$\angle BOC = \frac{1}{2} (180^\circ - \angle A)$$

 \Rightarrow

$$\angle BOC = 90^\circ - \frac{1}{2} \angle A = 90^\circ - \frac{1}{2} \angle BAC$$

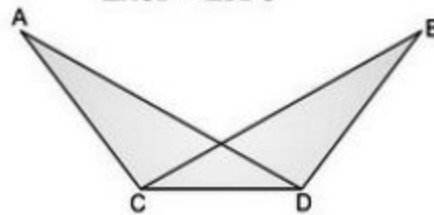
 $\frac{1}{2}$

[CBSE Marking Scheme, 2012]

29.

$$\begin{aligned}\angle BCD + \angle ACB &= \angle ADC + \angle BDA \\ \angle ACD &= \angle BDC\end{aligned}$$

1

In $\triangle ACD$ and $\triangle BDC$,

$$\angle BCD = \angle ADC$$

Given

$$\angle ACD = \angle BDC$$

1

$$DC = DC$$

1

 \Rightarrow

$$\triangle ACD \cong \triangle BDC$$

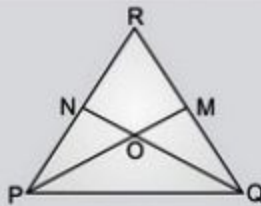
(By ASA)

 \Rightarrow

$$A = \angle B \text{ and } AD = BC$$

(By c.p.c.t.) 1

30.



$$RP = RQ$$

(Given)

 \Rightarrow

$$\angle RQP = \angle RPQ$$

(Proved) 1

 \Rightarrow

$$\angle MQP = \angle NPQ$$

In $\triangle PQN$ and $\triangle QPM$,

$$\angle NPQ = \angle MQP$$

1

$$PN = QM$$

(Given)

$$PQ = PQ$$

(Common)

 \therefore

$$\triangle PQN \cong \triangle QPM$$

(By SAS) 1

 \Rightarrow

$$\angle PQN = \angle QPM$$

(By c.p.c.t.)

 \Rightarrow

$$\angle PQO = \angle QPO$$

1

 \Rightarrow

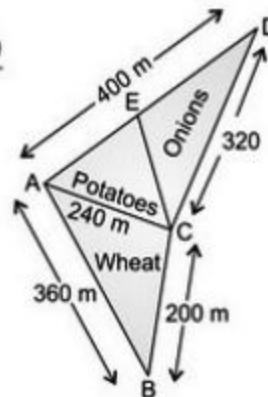
$$OP = OQ \text{ (Sides opposite to equal angles are equal) Proved.}$$

[CBSE Marking Scheme, 2012]

31. Let ABC be the triangular field where wheat is grown. Let ACD be the adjacent field which has been divided in two parts by joining C to the mid-point of AD .

For area of $\triangle ABC$

$$\begin{aligned}S &= \frac{AB + BC + CA}{2} \\ &= \frac{360 + 200 + 240}{2}\end{aligned}$$



$$\begin{aligned}
 &= 400 \text{ m} \\
 \text{Area of } \triangle ABC &= \sqrt{s(s-a)(s-b)(s-c)} \\
 &= \sqrt{400(400-360)(400-200)(400-240)} \\
 &= \sqrt{400 \times 40 \times 200 \times 160} \\
 &= 16000 \times \sqrt{2} \text{ m}^2 && \frac{1}{2} \\
 &= 1.6 \times \sqrt{2} \text{ hectares} && \frac{1}{2} \\
 &= 2.26 \text{ hectares.}
 \end{aligned}$$

Hence, area used for growing wheat = area of $\triangle ABC$
 $= 2.26$ hectares.

Again since CE is a median of $\triangle ACD$

\therefore It divides $\triangle ACD$ in two triangles of equal area

i.e. area of $\triangle ACE$ = area of $\triangle CDE$ $\frac{1}{2}$

For area of $\triangle ACD$ $s = \frac{AC + CD + DA}{2}$

$$\begin{aligned}
 &= \frac{240 + 320 + 400}{2} \\
 &= 480 \text{ m}
 \end{aligned}$$

Area of $\triangle ACD$ $= \sqrt{s(s-a)(s-b)(s-c)}$ $\frac{1}{2}$

$$\begin{aligned}
 &= \sqrt{480(480-240)(480-320)(480-400)} \\
 &= \sqrt{480 \times 240 \times 160 \times 80} \\
 &= 3.84 \text{ hectares}
 \end{aligned}$$

So, area of $\triangle ACE$ = area of $\triangle CDE$ $\frac{1}{2}$

$$\begin{aligned}
 &= \frac{1}{2} \times \text{area of } \triangle ACD && \frac{1}{2} \\
 &= \frac{3.84}{2} \\
 &= 1.92 \text{ hectares} && \frac{1}{2}
 \end{aligned}$$

Hence area used for growing potatoes = area of $\triangle ACE$
 $= 1.92$ hectares.

and area used for growing onions = area of $\triangle CDE$
 $= 1.92$ hectares. $\frac{1}{2}$







[NCERT Video and Text solutions](#)
 [Interactive Concept Videos](#)
 [Solved Sample Papers \(Text and Video\)](#)
 [Discussion Forum](#)
 [Vedic Mathematics](#)

LearnCBSE.in

Never Stop Learning


<https://plus.google.com/+phanicbse>


facebook.com/ncertsolutionsbooks


<https://in.pinterest.com/LearnCBSE/>


<https://twitter.com/learnCBSE>